Philosophy 134 Spring, 2005 Homework 7

Due: June 1, 2005, in class

- 1. Explain why the semantics for *S5I* without possible worlds yields the same consequence relations as the semantics in which accessibility is a universal relation.
- 2. Using the semantics without possible worlds, prove the following in *S5I*: $\models_{S5I} \Diamond (P \land \Box Q) \equiv (\Diamond P \land \Box Q)$.
- 3. Using the semantics with possible worlds and without the accessibility relation, show that the following is a semantical entailment in *S5I*: $\{\lozenge \Box \lozenge P\} \models_{S5I} \lozenge P$.
- 4. Show that *S4.3I* contains *S4.2I* by showing that if the accessibility relation is reflexive, transitive, and connected, then it is reflexive, transitive, and convergent.
- 5. Explain why in *PLI* if a sentence is satisfied by at least one variable assignment, it is satisfied by all variable assignments.